

# Multiplying Polynomials

Monomial (one term) times Binomial (two terms):

Simplify:  $5(2x + 7)$

$$\begin{aligned} & 5 \cdot 2x + 5 \cdot 7 \\ & 10x + 35 \end{aligned}$$

Example  
Distributive property  
Multiplication of factors

Simplify:  $(5x - 3)(-4y)$

$$\begin{aligned} & (-4y)(5x) - (-4y)(3) \\ & -20xy + 12y \end{aligned}$$

Example  
Distributive property  
Multiplication of factors

Binomial (2 terms) times Binomial (2 terms):

Simplify:  $(2x + 7)(5x + 3)$

1. Multiply First terms  
2. Multiply Outside terms  
3. Multiply Inside terms  
4. Multiply Last terms

$$\begin{array}{cccccc} \underline{2x} \cdot \underline{5x} & + & \underline{2x} \cdot \underline{3} & + & \underline{7} \cdot \underline{5x} & + \underline{7} \cdot \underline{3} \\ \text{First} & & \text{Outside} & & \text{Inside} & \text{Last} \end{array} \quad \begin{array}{l} \text{Distributive property} \\ \text{Spells "FOIL"} \end{array}$$

**Did you notice that the first letter of each word F-O-I-L spells FOIL???**  
**This is a trick to help you remember the steps to multiplying 2 binomials!**

$$\begin{aligned} & 10x^2 + 6x + 35x + 21 && \text{Multiplication of factors} \\ & 10x^2 + 41x + 21 && \text{Addition of like terms} \end{aligned}$$

**Binomial (2 terms) times Binomial (2 terms) continued:**

These problems use the same method as on the previous page.  
But they **LOOK** different because there is no middle term!

Simplify:  $(5x + 2)(5x - 2)$

$$5x \cdot 5x - 5x \cdot 2 + 5x \cdot 2 - 2 \cdot 2$$

$$25x^2 - 10x + 10x - 4$$

$$25x^2 - 4$$

Example

Distributive property

Multiplication of factors

Combine like terms

**Difference of squares**

Note: This answer is called:  
because it is subtraction and both terms are perfect squares.

Simplify:  $(x + 4)^2$

$$x^2 + 8x + 16$$

**MEANS**  $(x + 4)(x + 4)$

**Distribute:**

1.  $3(2x + 5)$
2.  $8(3x - 2)$
3.  $-4(5x + 3)$
4.  $-5(2x - 5)$
5.  $(3x - 2)(-6)$
6.  $3x(5x + 2)$
7.  $-2x(7x - 4)$
8.  $5y(2x + 3m + 6)$
9.  $(-x + 5r^2 - 7)(-2)$
10.  $4x + 5(2y + 3)$

**Answers:**

- $6x + 15$
- $24x - 16$
- $-20x - 12$
- $-10x + 25$
- $-18x + 12$
- $15x^2 + 6x$
- $-14x^2 + 8x$
- $10xy + 15my + 30y$
- $2x - 10r^2 + 14$
- $4x + 10y + 15$

The  $4x$  is a separate term and not part of the distributive property!

11.  $(x + 5)(x + 3)$
12.  $(3x + 5)(-2x + 1)$
13.  $(2x + 3)(4m + 5)$
14.  $(3x - 2)(2x - 5)$
15.  $(5x^2 + 8)(2x - 3)$
16.  $(4x - 3)(4x + 3)$
17.  $(5y + 4)(5y - 4)$
18.  $(2x - 5)^2$
19.  $(7m + 3)^2$

- $x^2 + 8x + 15$
- $-6x^2 - 7x + 5$
- $8mx + 10x + 12m + 15$
- $6x^2 - 19x + 10$
- $10x^3 - 15x^2 + 16x - 24$
- $16x^2 - 9$
- $25y^2 - 16$
- $4x^2 - 20x + 25$
- $49m^2 + 42m + 9$